

AIRCRAFT DESIGN AND SYSTEMS GROUP (AERO)

## Understanding the Aircraft Mass Growth and Reduction Factor

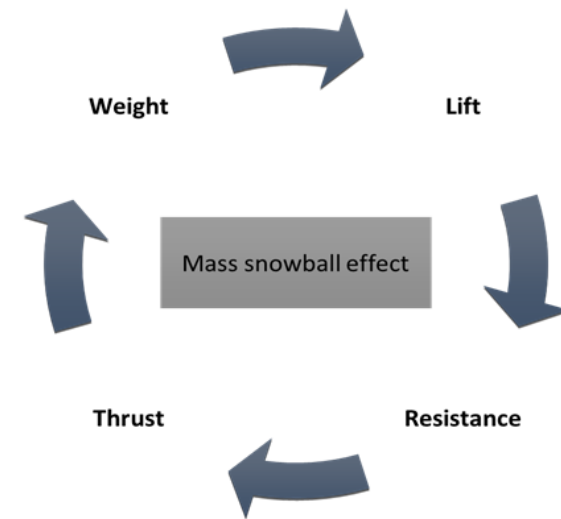
Dieter Scholz

Hamburg University of Applied Sciences

EWADE 2020 - 15th European Workshop on Aircraft Design Education

READ 2020 - Research and Education in Aircraft Design

Online, 21<sup>st</sup> and 22<sup>nd</sup> October 2020



Initially a short message:

Continuous Special Issue  
**"Aircraft Design"**  
of the Open Access Journal  
**"Aerospace"** at  
**MDPI**

Continuous Special Issue "Aircraft Design" of the Open Access Journal "Aerospace" at MDPI

## "Aircraft Design" our "Journal"

**Purpose** – Establish a "journal" for the aircraft design community.

**Approach** – Aircraft design is too small as a topic for a journal. Use a continuous Special Issue i.e. **only a subset of a journal**. Follow the Open Access publishing model that can live already on a low number of papers annually.

**Findings** – The **well established publisher MDPI** published already one Special Issue "Aircraft Design" in "Aerospace" (ISSN 2226-4310) and was willing to follow the approach. The journal has a CiteScore (2019) of 2.6 from **Scopus** and is part of the Emerging Sources Citation Index - **Web of Science** (Clarivate Analytics).

**Tradition** – The **tradition** of the journal Aircraft Design at Elsevier (ISSN: 1369-8869) which was published from 1998 to 2002 with **Prof. Egbert Torenbeek** and **Prof. Dr. Jan Roskam** as Editors is continued.

**Limitations** – **Article Processing Charges (APC)** have to be paid. A **30% discount is available for authors from EWADE and READ**. Further discounts are granted based on reviews.

**Originality and Value** – This is the only "journal" fully dedicated to aircraft design.

## Continuous Special Issue "Aircraft Design" of the Open Access Journal "Aerospace" at MDPI

<http://journal.AircraftDesign.org>

Aerospace (ISSN 2226-4310) - An Open Access Journal

with [Special Issue](#)

### Aircraft Design

Usually special issues of a journal are introduced for "hot topics" and are titled as such. The idea is here, to use the subset "Special Issue" of the journal "Aerospace" at MDPI for a specialized scientific domain - Aircraft Design.

**Closing Date:** The current special issue (SI-2/2020) has a closing date of 31 December 2020.

**Keywords:** aircraft, design, OAD, configuration, requirements, payload, range, certification, safety, constraints, objectives, synthesis, optimization, aerodynamics, drag, high-lift, structure, mass, performance, stability, control, aeroelasticity, engine, systems, operating costs, DOC, passenger, cabin, ticket, price, environment, profit, asset, wing, fuselage, tail, undercarriage, landing gear, engine, systems.

**Paper Type and Content:** In addition to original research articles also review papers, letters or communications, technical reports, and extended version of conference papers are accepted. An interest exists also in aircraft design education.

**High Visibility:** Papers will be visible [Open Access](#) at the journal "Aerospace" and also alongside the Special Issue "Aircraft Design" as soon as they are ready. The journal "Aerospace" is covered by many [databases and archives](#) including [Web of Science](#) (Clarivate Analytics) and [Scopus](#) (Elsevier).

**Rapid Publication:** Manuscripts at the journal "Aerospace" are peer-reviewed and a first decision provided to authors approximately 18 days after submission; acceptance to publication is undertaken in 6.3 days. Once accepted, the manuscripts undergo professional copy-editing, proofreading by the authors, final corrections, and publication on the [www.mdpi.com](http://www.mdpi.com) website.

**Tradition:** The current Special Issue [Aircraft Design \(SI-2/2020\)](#) follows the Special Issue [Aircraft Design \(SI-1/2017\)](#) and continues the tradition of the journal [Aircraft Design](#) (ISSN: 1369-8869), which Prof. Egbert Torenbeek had started together with Prof. Dr. Jan Roskam as Editors at Elsevier in 1998. The subscription-based publishing model proved inadequate to serve the rather small aircraft design community. For this reason, the Elsevier title had to be [discontinued in 2002](#). This pitfall is avoided with the [Open Access](#) publishing model used by MDPI for all its journals including this Special Issue.

**Article Processing Charges (APC):** 1000 CHF. A 30% discount applies for authors from EWADE / SCAD / TCAD (1). Reviewers who provide timely, thorough peer-review reports receive vouchers entitling them to an additional discount on the APC of their next publication. This means APC can be reduced to a bearable amount, which is usually acceptable to the author's institution.

Guest Editor

Prof. Dr. Dieter Scholz



[Website](#) [E-Mail](#)

Honorary Guest Editor

Prof. em. Egbert Torenbeek



[Website](#)



## Special Issue Editors

Dieter Scholz



Egbert Torenbeek



## Continuous Special Issue "Aircraft Design" of the Open Access Journal "Aerospace" at MDPI

# The Editorial Explains the Setup

Dieter Scholz:

**Publishing in "Aircraft Design" with a Continuous Open Access Special Issue**

<https://doi.org/10.3390/aerospace7010005>



**aerospace**  
an Open Access Journal by MDPI

**Aircraft Design (SI - 2 / 2020)**

**Guest Editors**  
Prof. Dr. Dieter Scholz, Prof. em. Egbert Torenbeek

**Deadline**  
31 December 2020

[mdpi.com/si/25829](https://www.mdpi.com/si/25829)

**Special Issue**  
Invitation to submit

**CITESCORE 1.57**  
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**Aerospace**  
(ISSN 2226-4310)  
<https://www.mdpi.com/journal/aerospace>  
<https://doi.org/10.3390/aerospaceVMMxxxx>

**Continuous Special Issue Aircraft Design**  
[https://www.mdpi.com/journal/aerospace/special\\_issues/aircraft\\_design](https://www.mdpi.com/journal/aerospace/special_issues/aircraft_design)

<p><b>SI-1/2017</b> <a href="https://www.mdpi.com/si/6497">https://www.mdpi.com/si/6497</a></p> <p>Articles: <a href="https://doi.org/10.3390/aerospace3040035">aerospace3040035</a> <a href="https://doi.org/10.3390/aerospace3040038">aerospace3040038</a> <a href="https://doi.org/10.3390/aerospace4010006">aerospace4010006</a> <a href="https://doi.org/10.3390/aerospace4030035">aerospace4030035</a> <a href="https://doi.org/10.3390/aerospace4030037">aerospace4030037</a></p>	<p><b>SI-2/2020</b> <a href="https://www.mdpi.com/si/25829">https://www.mdpi.com/si/25829</a></p> <p>Articles: <a href="https://doi.org/10.3390/aerospace6060067">aerospace6060067</a> <a href="https://doi.org/10.3390/aerospace6110122">aerospace6110122</a></p> <p>...</p>	<p><b>SI-3/20xx</b> <a href="https://www.mdpi.com/si/xxxx">https://www.mdpi.com/si/xxxx</a></p> <p>Articles: aerospaceVMMxxxx aerospaceVMMxxxx</p> <p>...</p>
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**Aircraft Design (SI - 1 / 2017)**

**Guest Editor**  
Dr. Mohammad Sadraey

**Deadline**  
31 May 2017

[mdpi.com/si/6497](https://www.mdpi.com/si/6497)

**Special Issue**  
Invitation to submit

Continuous Special Issue "Aircraft Design" of the Open Access Journal "Aerospace" at MDPI

## The Publisher: MDPI



MDPI Headquarters, Basel

MDPI is a member of



Continuous Special Issue "Aircraft Design" of the Open Access Journal "Aerospace" at MDPI

## The Publisher: MDPI



MDPI Office in Wuhan, China



Now to my presentation:

# Understanding the **Aircraft Mass Growth and Reduction Factor**



## Understanding the Aircraft Mass Growth and Reduction Factor

### Abstract

**Purpose** – This project work shows a [literature survey](#), clearly defines the mass growth factor, shows a mass growth iteration, and derives an [equation for a direct calculation of the factor](#) (without iteration). Definite values of the factor seem to be missing in literature. To change this, [mass growth factors are being calculated for](#) as many of the prominent passenger aircraft as to cover [90% of the passenger aircraft](#) flying today. The dependence of the mass growth factor on requirements and technology is examined and the relation to Direct Operating Costs (DOC) is pointed out.

**Methodology** – [Calculations start from first principles](#). Publically available data is used to calculate a list of mass growth factors for many passenger aircraft. Using equations and the resulting relationships, new knowledge and dependencies are gained.

**Findings** – The mass growth factor is larger for aircraft with larger operating empty mass ratio, smaller payload ratio, larger specific fuel consumption (SFC), and smaller glide ratio. [The mass growth factor increases much with increasing range](#). The factor depends on an increase in the fixed mass, so this is the same for the payload and empty mass. The mass growth factor [for subsonic passenger aircraft is on average 4.2](#), for narrow body aircraft 3.9 and for wide body aircraft (that tend to fly longer distance) 4.9. In contrast supersonic passenger aircraft show a factor of about 14.

**Practical implications** – The mass growth factor has been revisited in order to [fully embrace the concept of mass growth](#) and may lead to a better general understanding of aircraft design.

**Social implications** – A detailed [discussion of aircraft costs](#) as well as aircraft development requires detailed knowledge of the aircraft. By understanding the mass growth factor, consumers can have this discussion with industry at eye level.

**Originality/value** – The [derivation of the equation for the direct calculation of the mass growth factor](#) and the determination of the factor [using the method for 90% of current passenger aircraft](#) was not shown.

## Understanding the Aircraft Mass Growth and Reduction Factor

# Acknowledgment

This presentation is based on the project of

**John Singh Cheema**

prepared at

Hamburg University of Applied Sciences

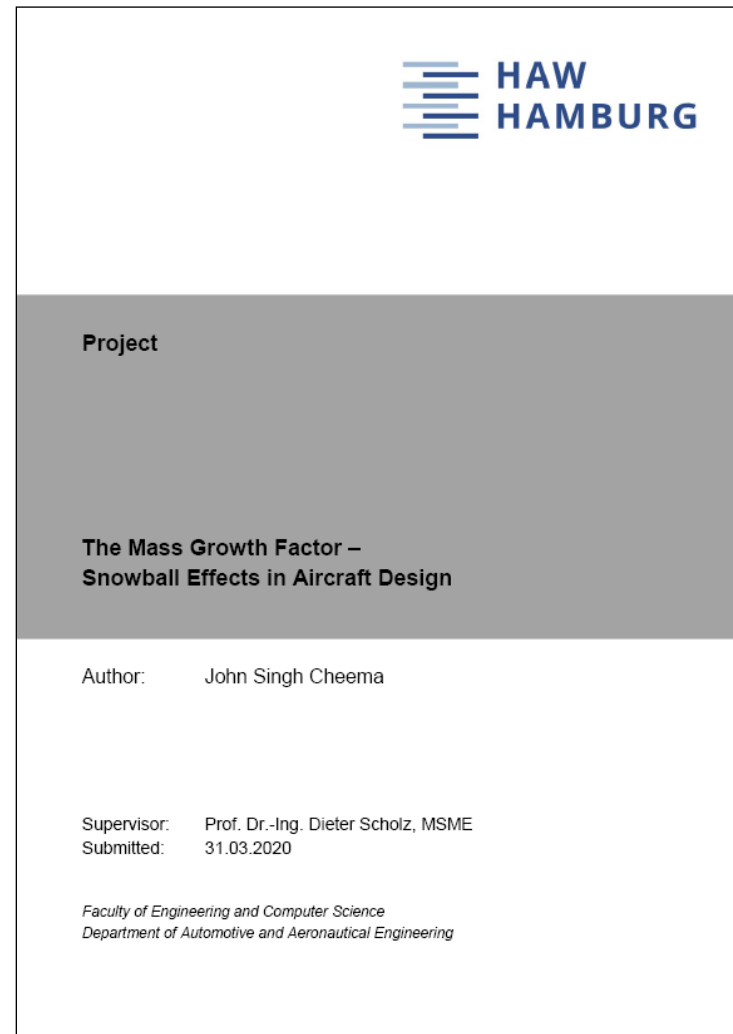
Aircraft Design and Systems Group (AERO)


Download from:

<http://library.ProfScholz.de>

Referenced here as:

**Cheema 2020**



 HAW  
HAMBURG

**Project**

**The Mass Growth Factor –  
Snowball Effects in Aircraft Design**

Author: John Singh Cheema

Supervisor: Prof. Dr.-Ing. Dieter Scholz, MSME  
Submitted: 31.03.2020

*Faculty of Engineering and Computer Science  
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## Understanding the Aircraft Mass Growth and Reduction Factor

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- **Mass Growth Factor**
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  - **Obtained from Technology and Range**
  - **Linked to Direct Operating Costs (DOC)**
- Summary

## Background

- The aircraft mass growth factor is fundamental to aircraft preliminary design. Due to the fact that **mass during some aircraft design phases seems rather to increase** than to decrease compared to initial estimates, the factor is called **mass growth factor**.
- However, a mass reduction factor is mathematically the same. The **mass reduction factor** can lead to even substantial mass reduction and is as such the secret to efficient aircraft design. **For simplicity and tradition we may just talk about mass growth**.
- It is usually **defined as the ratio of an increase in the total mass (take-off mass) due to an arbitrary increase in local mass (empty mass)** determined after a full iteration in aircraft design to achieve the original performance requirements (payload and range).
- The aircraft design iteration sees after each loop another increment in the take-off mass, so that an initial (local) mass increase aggravates the situation like a snow ball transforming into an **avalanche**. Hence the pseudonym **snowball factor**.
- The concept of the mass growth factor is probably as old as aviation. It has been **discussed heavily from the 1950th to the 1970th** and has continued to be mentioned until today. Nevertheless, it seems not to be well enough understood today. Maybe its importance has declined due to **modern computing power** providing quite accurate mass estimates in each design phase, but **detaching the engineer from the feel for the numbers**.

## Avalanche – Snow Ball Effect



Avalanche by Dahu1, wikimedia.org, CC BY-SA

## Literature Review (Overview)

Ballhaus 1954	(SAWE Paper)
Saelman 1973	(SAWE Paper)
Fürst 1999	(LTH, Germany)
Sinke 2019	(Lecture Notes, TU Delft)
SAWE 2019	(SAWE Book)



elaborate the principle

### Aircraft Design Books

Torenbeek 1976  
 Roskam 1989  
 Jenkinson 1999  
 Howe 2000  
 Müller 2003



talk about design aspects

See **Cheema 2020** for details.

SAWE: Society of Allied Weight Engineers  
 LTH: Luftfahrttechnisches Handbuch

## Literature Review (Overview)

CLEAR DESIGN THINKING USING THE AIRCRAFT GROWTH FACTOR

By

Wm. F. Ballhaus

TO BE PRESENTED AT THE SAE NATIONAL AERONAUTICAL MEETING

Los Angeles, California

October 8, 1954

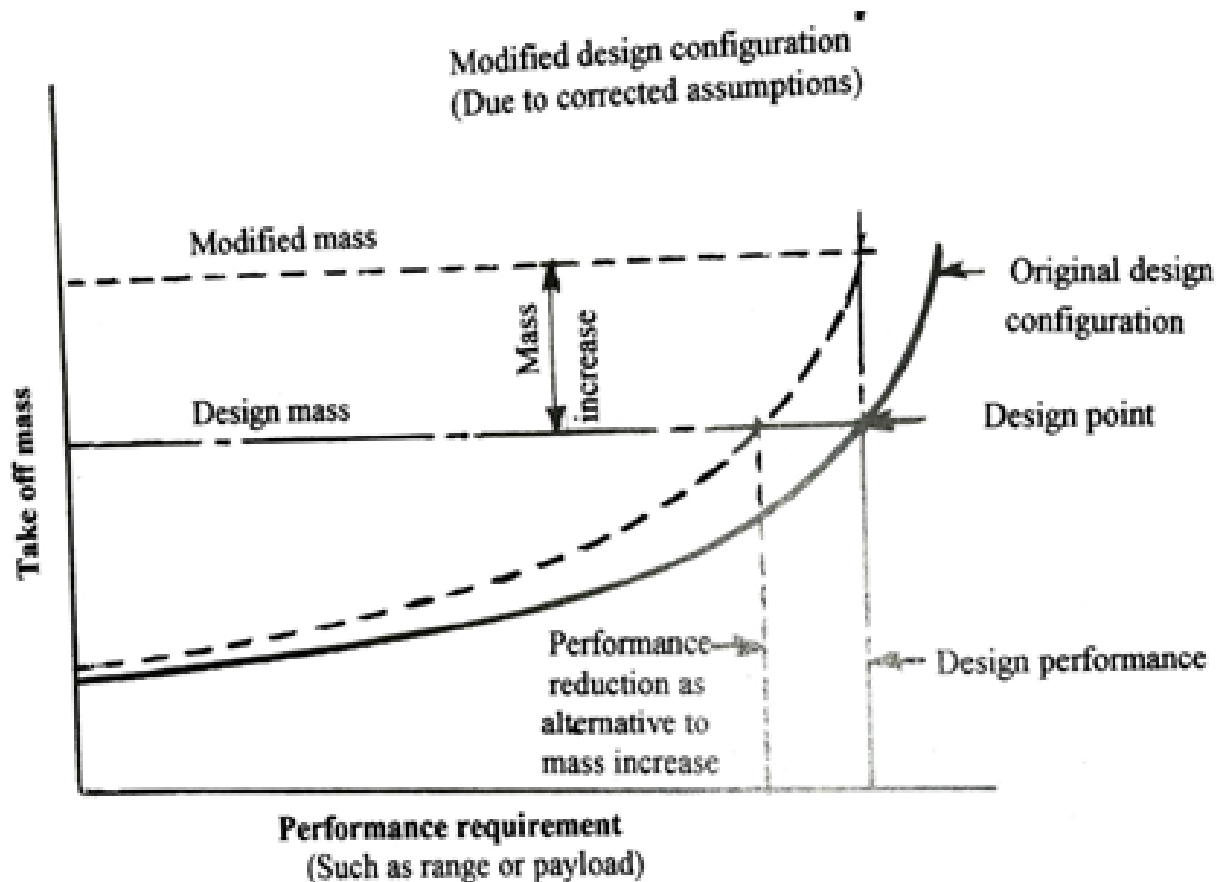
## Definition

$$G = \frac{\text{Change in Gross Weight}}{\text{Fixed Weight Added or Change in Fixed Weight}}$$

Ballhaus 1954



# Aircraft Design Mass Growth (Overall Picture)



New curve may become asymptotic at a mass less than the design value

Howe 2000

## Iteration of the Mass Growth Factor (Equations)

$$\Delta m_L = 1 \text{ kg}$$

$$m_{MTO,0} = m_{MTO} + \Delta m_G = m_{MPL} + m_{OE} + \Delta m_L + m_F$$

$$m_{MTO,1} = m_{MPL} + \frac{m_{OE}}{m_{MTO}} \cdot m_{MTO,0} + \Delta m_L + \frac{m_F}{m_{MTO}} \cdot m_{MTO,0}$$

■ ■ ■

$$\Delta m_G = m_{MTO,X} - m_{MTO}$$

$$k_{MGW} = \frac{\Delta m_G}{\Delta m_L}$$

$m_F$	Fuel Mass
$m_{MPL}$	Maximum Payload
$m_{PL}$	Payload
$m_{MTO}$	Maximum take-off mass
$m_{OE}$	Operating empty mass
$\Delta m_L$	Local mass growth
$\Delta m_G$	Global mass growth
$k_{MGW}$	Mass growth factor

# Iteration of the Mass Growth Factor (Excel Table)

Mass Growth Factor by Iteration						
Local Mass Growth	DmL	1	kg			
Maximum take-off mass	mMTO	73000	kg			
Operating empty mass fraction	mOE/mMTO	0.5				
Operating empty mass	mOE	36500	kg			
Fuel mass fraction	mF/mMTO	0.25				
Fuel mass fraction	mF	18250	kg			
Maximum Payload	mMPL	18250	kg			

Iteration							Determination of mass fraction	
i	mMTO,i	Global mass growth: DmG	Change	DmG/DmL	kMGW			
0	73001.000 kg	1.00000			4.00			
1	73001.750 kg	1.75000	75.0000%	1.75000		$m_{MTO}$	73000 kg	
2	73002.313 kg	2.31250	32.1429%	2.31250		$m_{PL}$	18250 kg	
3	73002.734 kg	2.73438	18.2432%	2.73438		$m_{OE}$	36500 kg	
4	73003.051 kg	3.05078	11.5714%	3.05078		$m_F$	18250 kg	
5	73003.288 kg	3.28809	7.7785%	3.28809		$m_{PL}/m_{MTO}$	0.250	
6	73003.466 kg	3.46606	5.4128%	3.46606		$m_{OE}/m_{MTO}$	0.500	
7	73003.600 kg	3.59955	3.8512%	3.59955		$m_F/m_{MTO}$	0.250	
8	73003.700 kg	3.69966	2.7813%	3.69966				
9	73003.775 kg	3.77475	2.0295%	3.77475				
10	73003.831 kg	3.83106	1.4918%	3.83106				
11	73003.873 kg	3.87329	1.1024%	3.87329				
12	73003.905 kg	3.90497	0.8178%	3.90497				
13	73003.929 kg	3.92873	0.6084%	3.92873				
14	73003.947 kg	3.94655	0.4535%	3.94655				
15	73003.960 kg	3.95991	0.3386%	3.95991				
16	73003.970 kg	3.96993	0.2531%	3.96993				
17	73003.977 kg	3.97745	0.1893%	3.97745				
18	73003.983 kg	3.98309	0.1417%	3.98309				
19	73003.987 kg	3.98732	0.1062%	3.98732				
20	73003.990 kg	3.99049	0.0795%	3.99049				

1. For the iteration method, the masses must be researched and thus the mass fractions determined

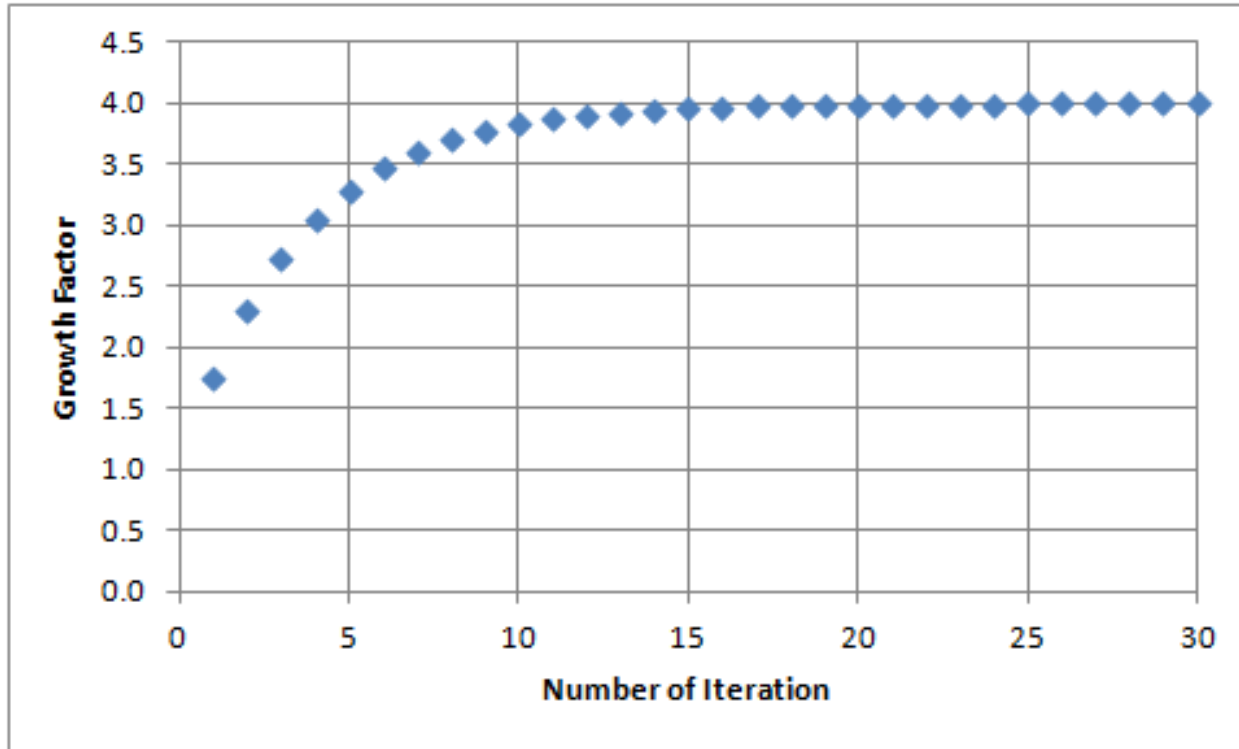
2. Enter the values in the blue fields

3. The iteration starts automatically and the mass growth factor is calculated



Data and tools uploaded to Harvard Dataverse: <https://doi.org/10.7910/DVN/6NHDDP>

# Iteration of the Mass Growth Factor (Convergence)



Convergence of the mass growth factor using the example of the Boeing 767-300

# Considering 90% of Passenger Aircraft

## World Fleet

Table A.1 90% of current aircraft (according to Robson 2019)

Aircraft Type	Number in Operation	Percent of total	Sum of most aircraft types in percent
Boeing 737-800	4804	16.83%	16.83%
A320	4135	14.48%	31.31%
A320neo	658	2.30%	33.61%
A321neo	160	0.56%	34.18%
A321	1650	5.78%	39.95%
Boeing 737 Max 8		0.00%	39.95%
A319	1249	4.37%	44.33%
Boeing 737-700	1005	3.52%	47.85%
ATR72	775	2.71%	50.56%
Boeing 777-300(ER)	829	2.90%	53.47%
Embraer 175	595	2.08%	55.55%
Boeing 787-9	451	1.58%	57.13%
A330-300	707	2.48%	59.61%
Boeing 767-300	622	2.18%	61.79%
A350-900	261	0.91%	62.70%
Boeing 757-200	600	2.10%	64.80%
A330-200	547	1.92%	66.72%
Boeing 737-900	550	1.93%	68.64%
De Havilland Canada Dash 8-400	502	1.76%	70.40%
Embraer 190	495	1.73%	72.14%
Boeing 737 Max TBD		0.00%	72.14%
Bombardier CRJ900	444	1.56%	73.69%
A220	77	0.27%	73.96%
Boeing 777-200	431	1.51%	75.47%
Embraer ERJ-145	422	1.48%	76.95%
Boeing 737 Max 10		0.00%	76.95%
Boeing 787-8	328	1.15%	78.10%

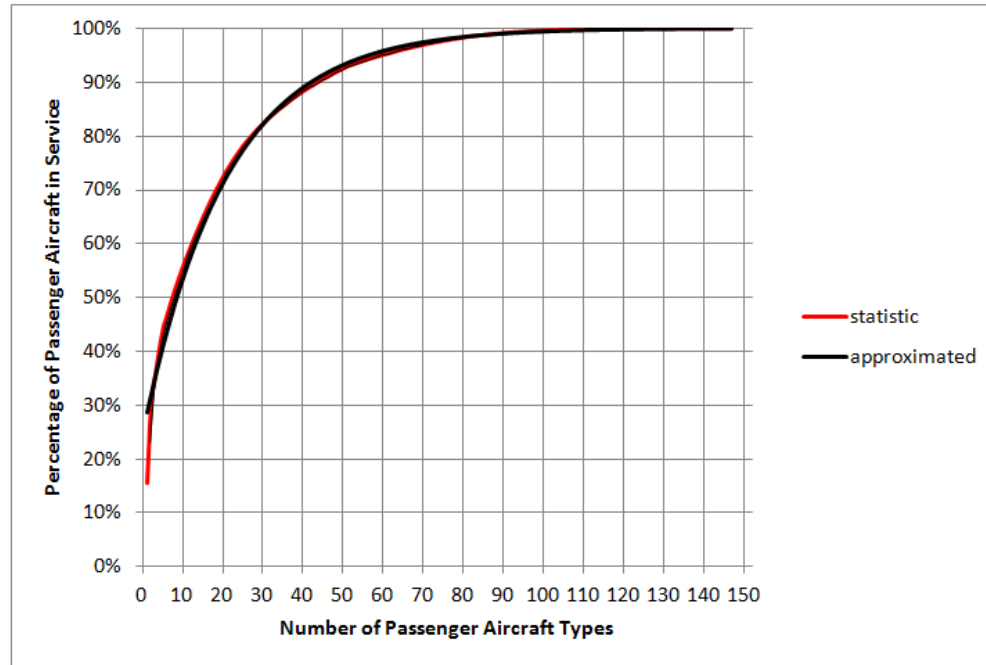
← e.g. 27 aircraft, 78.1% of fleet



# Considering 90% of Passenger Aircraft

$$\left( \frac{n}{n_{max}} \right)_{in\_service} = 1 - a \cdot e^{b \left( \frac{n}{n_{max}} \right)_{type}}$$

**a**      0.7480879  
**b**      -0.047978



with data from Flight 2016

# Mass Growth Factor – Considering 90% of Passenger Aircraft

**Table 3.3** Evaluation of 90% of all current flying commercial aircraft including two supersonic aircraft

Aircraft	$m_{MTO}$ [kg]	$m_{OE}$ [kg]	$m_{MPL}$ [kg]	$k_{MGW}$	Sources
Boeing 737-800	78220	41480	14690	<b>5.32</b>	Jenkinson 2019
A320-200	73500	42100	18633	<b>3.94</b>	Jackson 2011
A320neo	79000	44300	20000	<b>3.95</b>	Airbus 2005, Wiki 2020
A321neo	97000	50100	25500	<b>3.80</b>	Airbus 2005a, Wiki 2020
A321-200	89000	48000	22780	<b>3.90</b>	Jenkinson 2019
A319-100	64000	39200	17390	<b>3.68</b>	Jenkinson 2019
Boeing 737-700	69400	37585	11610	<b>5.97</b>	Jenkinson 2019
<b>ATR 72-500</b>	<b>22500</b>	<b>12950</b>	<b>7350</b>	<b>3.06</b>	Jackson 2011
Boeing 777-300 ER	299370	155960	68570	<b>4.36</b>	Jackson 2011
Embraer 175	37500	21810	9890	<b>3.79</b>	Jackson 2011
Boeing 787-9	244940	128850	52587	<b>4.65</b>	Boeing 2018, Wiki 2020c
A330-300	217000	118189	48400	<b>4.48</b>	Jenkinson 2019
Boeing 767-300	156489	87135	39140	<b>3.99</b>	Jenkinson 2019
A350-900	280000	142400	53300	<b>5.25</b>	Airbus 2005b, Wiki 2020a
Boeing 757-200	115900	58040	25690	<b>4.51</b>	Jenkinson 2019
A330-200	230000	120200	36400	<b>6.31</b>	Jenkinson 2019
Boeing 737-900	74389	42901	19831	<b>3.75</b>	Boeing 2013, Wiki 2020e
DHC Dash 8-400	24993	14968	7257	<b>3.44</b>	Lambert 1991
Embraer 190	50300	28080	13530	<b>3.71</b>	Jackson 2011
Bombardier CRJ900	36500	21430	10320	<b>3.53</b>	AirlinesInform 2020
A220-100	63049	35221	15127	<b>4.16</b>	Airbus 2019, Wiki 2020d
Boeing 777-200	242670	135875	54635	<b>4.44</b>	Jenkinson 2019

90% of aircraft considered globally with more than 19 seats by looking at 44 aircraft types.

**ATR 72:**  
propeller aircraft,  
short range

Cheema 2020

## Wisdom Gained

- 1.) Larger aircraft do not necessarily have a higher mass growth factor.
- 2.) It does not matter how large the local mass growth is; the mass growth factor remains unaffected.\*

$$m_{MTO} + \Delta m_G = m_{MPL} + m_{OE} + \Delta m_L + m_F$$

- 3.) It does not matter whether there is one kg more operating empty mass or one kg more payload on board. The mass growth factor for a growth in the operating empty mass is therefore the same factor as for a growth in the payload.
- 4.) Old long-range aircraft are more sensitive to local mass growth than new short-range aircraft.

\* This as long as the local mass growth is much smaller than the fixed mass. The position of the local mass growth does not matter, if the wing is not yet fixed and is positioned according to the new weight and balance situation.



# Mass Growth Factor – Aircraft Categories

**Table 4.1** Mass growth factor for different aircraft categories

Aircraft categories				
	Wide-Body	Narrow-Body	} Subsonic	Supersonic
$k_{MGW}$	4.91	3.85	} 4.23	13.82

## Mass Growth Factor – Obtained from Payload Fraction

After a longer derivation (Cheema 2020), we find a simple equation:

$$k_{MGW} = \frac{m_{MTO}}{m_{MPL}} = \frac{1}{1 - \frac{m_F}{m_{MTO}} - \frac{m_{OE}}{m_{MTO}}}$$

**Table 4.2** Mass growth factor for typical mass fractions

	Range type		
	Short-range	Medium-range	Long-range
$m_{OE}/m_{MTO}$	0.60	0.525	0.45
$m_F/m_{MTO}$	0.15	0.3	0.45
$k_{MGW}$	4	5.7	10

## Mass Growth Factor – Can Go to Infinity

$$k_{MGW} = \frac{m_{MTO}}{m_{MPL}} = \frac{1}{1 - \frac{m_F}{m_{MTO}} - \frac{m_{OE}}{m_{MTO}}}$$

As soon as

$$\left( \frac{m_F}{m_{MTO}} + \frac{m_{OE}}{m_{MTO}} \right)$$

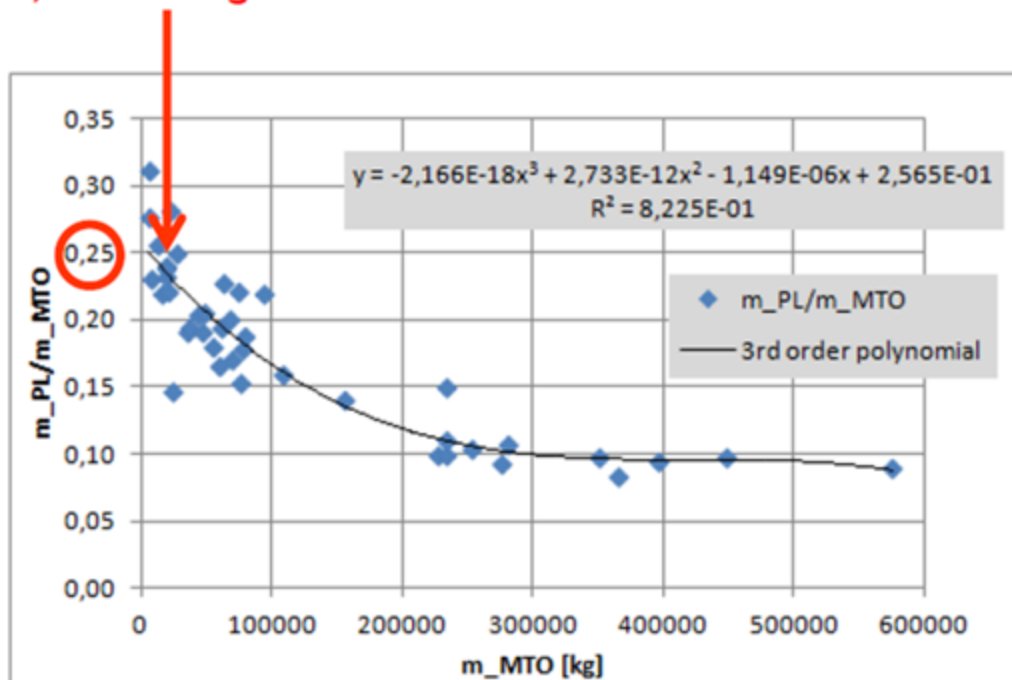
approaches 1.0 the mass growth factor,  $k_{MGW}$  goes towards infinity!

This means the design task has no solution!

# Mass Growth Factor – Payload Fraction from Statistics

$$k_{MGW} = \frac{1}{\frac{m_{MPL}}{m_{MTO}}}$$

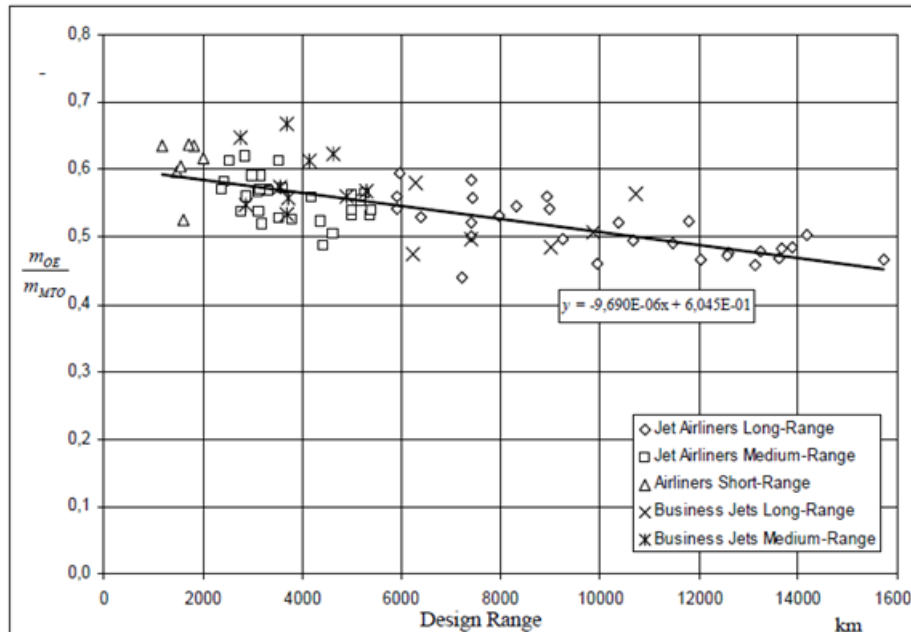
small A/C; short range



$$k_{MGW} = 4 \dots 10$$

Scholz 2018

# Mass Growth Factor – Obtained from Technology and Range



Scholz 2015

$c$	Specific fuel consumption
$R$	Range
$B$	Breguet factor
$E$	Glide ratio in cruise flight
$V$	Cruising speed

$$B = \frac{E \cdot V}{c \cdot g}$$

$$\frac{m_F}{m_{MTO}} = 1 - e^{-\frac{R}{B}}$$

$$\frac{m_{OE}}{m_{MTO}} = 0.5967 - 0.0000166(1/\text{NM}) \cdot R$$

Lehnert 2018

$$k_{MGW} = \frac{1}{1 - (0.5967 - 0.0000166(1/\text{NM}) \cdot R) - \left(1 - e^{-\frac{R}{B}}\right)}$$

# Mass Growth Factor – Linked to Direct Operating Costs (DOC)

Seat-Mile-Costs:

$$C_{s,m} = \frac{C_{a/c,t}}{R \cdot n_s} = \frac{C_{a/c,a}}{R \cdot n_s \cdot n_{t,a}}$$

$DOC = C_{DOC} = C_{a/c,a}$

← depends on cruise speed (given)  
← range (given)

$$DOC \approx m_{MTO} = m_{OE} + m_F + m_{PL}$$

← payload (given, constant)  
← fuel costs  
← depreciation, maintenance costs

$$\frac{DOC}{n_s} \approx \frac{m_{MTO}}{m_{PL}} = \frac{1}{\frac{m_{PL}}{m_{MTO}}} = k_{MGW}$$

$C_{a/c,a}$	Aircraft annual costs
$n_{t,a}$	Number of Flights per year
$C_{s,m}$	Seat-mile costs
$C_{a/c,t}$	Aircraft trip cost

## Summary

- The mass growth (and reduction) factor is well known, but not well understood:
  - Derivation missing => added
  - Numerical values missing => added
- Average value for subsonic passenger aircraft: 4.2  
range from 3.1 (ATR-72) via 6.2 (A380) and 6.5 (B747-400) to 15.6 (Concorde)
- The mass growth factor important for the design phase (snow ball effect) and also a good indicator to quickly understand the aircraft's economy.
- The mass growth factor can be estimated from basic parameters: range,  $R$ ;  $E = L/D$ ;  $c = \text{SFC}$ ; cruise speed,  $V$ :

$$k_{MGW} = \frac{1}{\frac{m_{MPL}}{m_{MTO}}}$$

$$k_{MGW} = \frac{1}{1 - (0.5967 - 0.0000166(1/\text{NM}) \cdot R) - \left(1 - e^{-\frac{R}{B}}\right)}$$

$$B = \frac{E \cdot V}{c \cdot g}$$

## Understanding the Aircraft Mass Growth and Reduction Factor

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