



Reverse Engineering of Passenger Jets – Classified Design Parameters

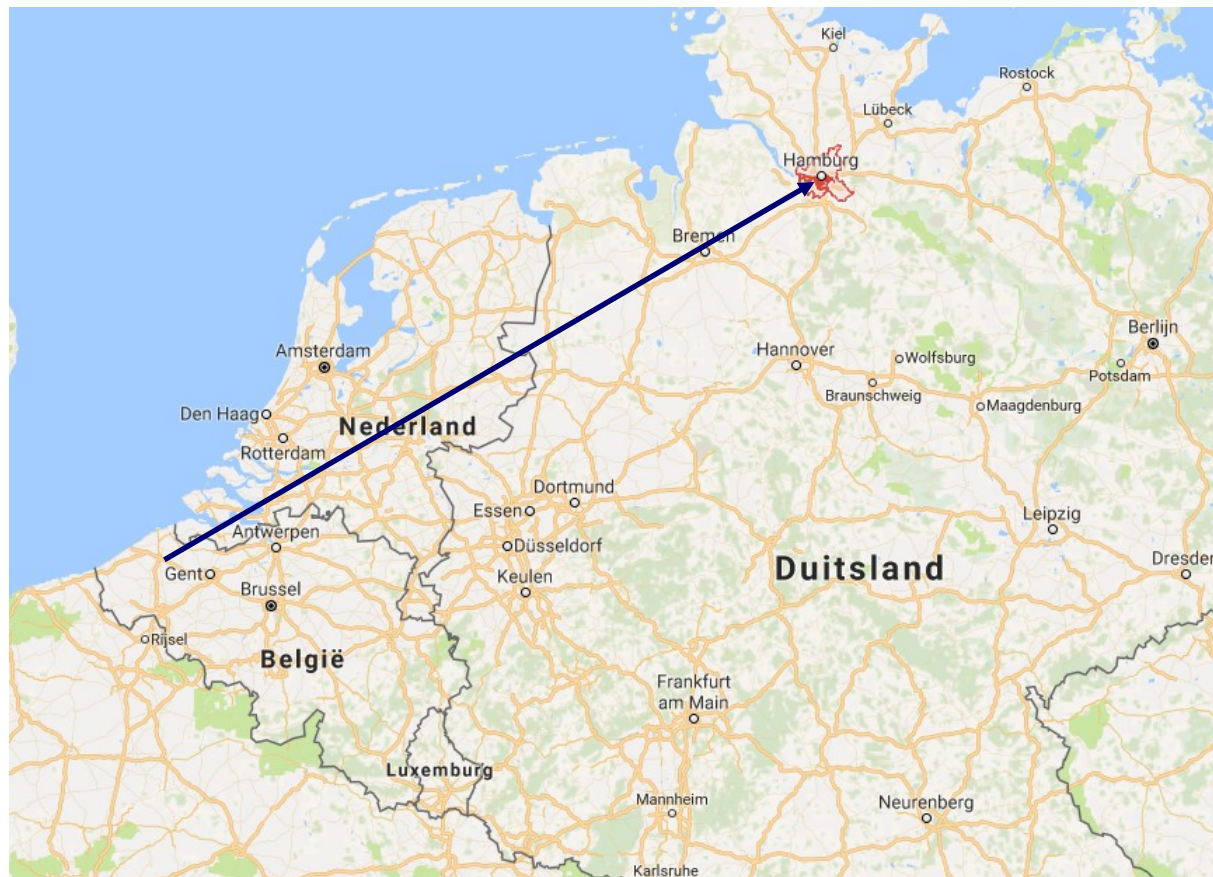
Emiel De Grave

Examiner: Prof. Dr.-Ing Dieter Scholz, MSME

August 2017

Reverse Engineering of Passenger Jets – Classified Design Parameters

Erasmus Hamburg (Germany)





Reverse Engineering of Passenger Jets – Classified Design Parameters

Master Thesis

Reverse Engineering

Passenger Jets

Classified

Design Parameters

Reverse Engineering of Passenger Jets – Classified Design Parameters

Design Parameters

Maximum lift coefficient: $C_{L,max}$

- Landing
- Take-off

Lift-to-drag ratio: E

Specific fuel consumption: SFC



Reverse Engineering of Passenger Jets – Classified Design Parameters

Content

1. Preliminary Sizing of Passenger Aircraft
2. Concept Reverse Engineering
3. Reverse Engineering of Preliminary Sizing
4. Tool
5. Example



Preliminary Sizing of Passenger Aircraft

Aircraft design parameters

- Take-off mass
- Fuel mass
- Operating empty mass
- Wing area
- Take-off thrust

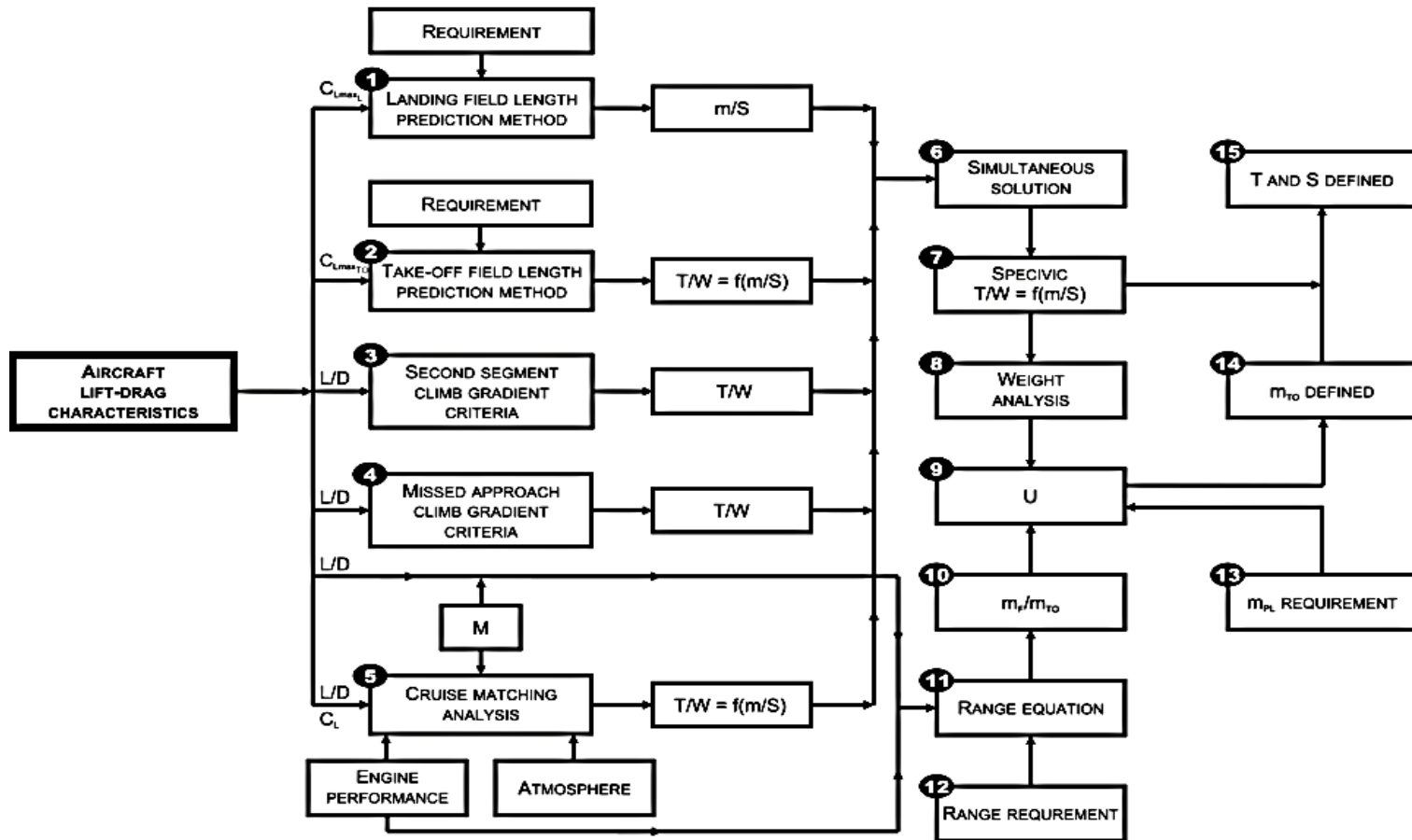


Preliminary Sizing of Passenger Aircraft

1. Landing
2. Take-off
3. Second Segment
4. Missed Approach
5. Cruise

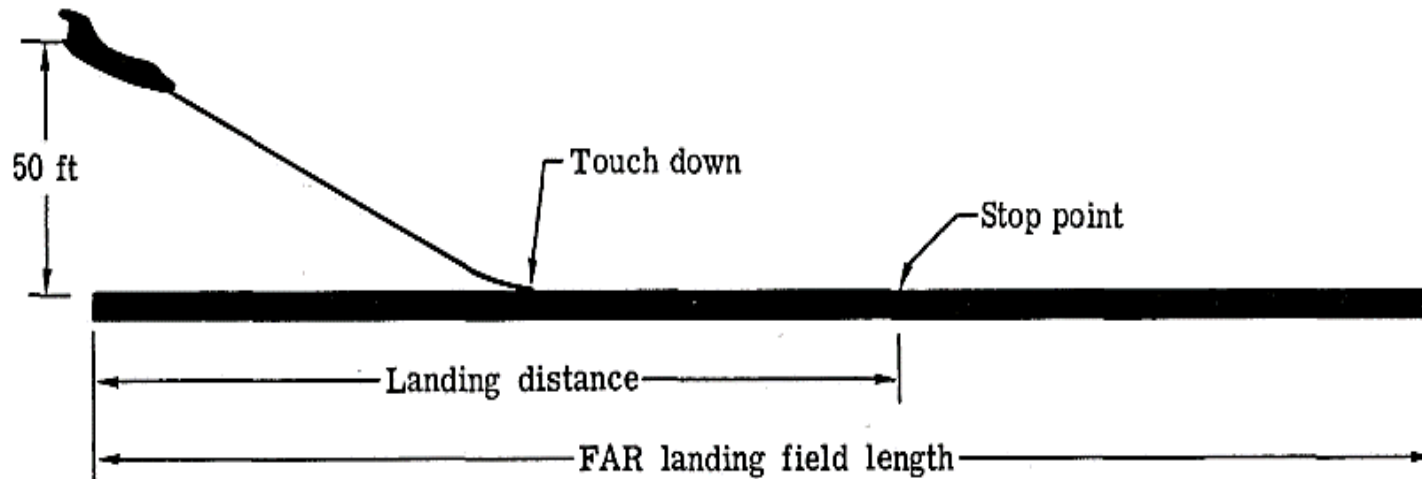
Acc. to Federal Air Regulations (FAR Part 25)

Preliminary Sizing of Passenger Aircraft



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Preliminary Sizing – Landing

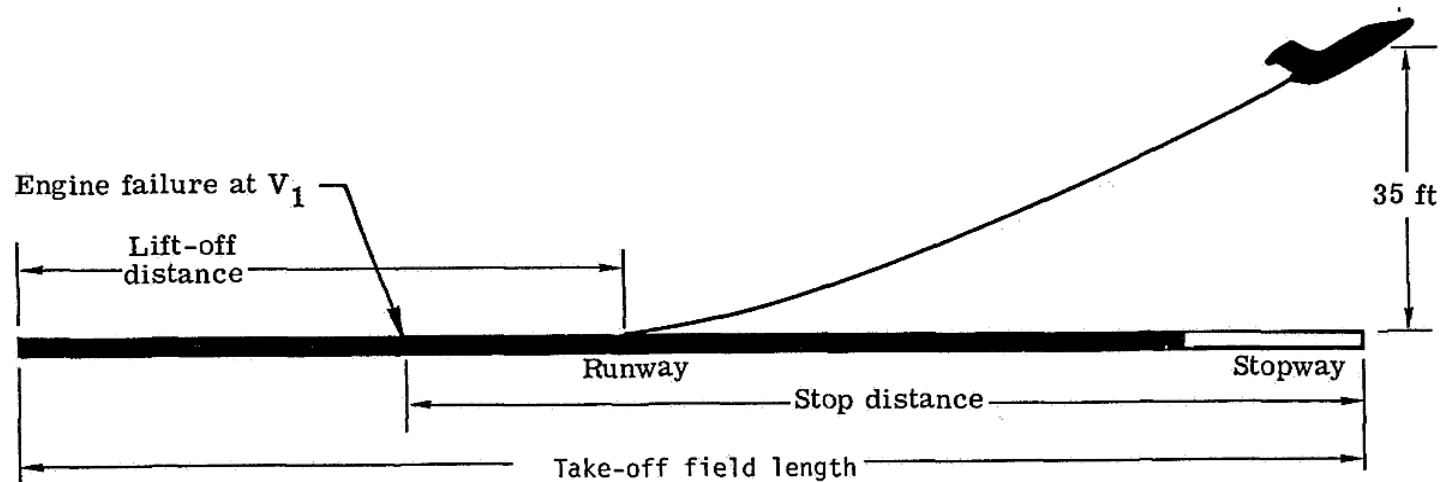


$$\frac{m_{MTO}}{S_W} = k_L \cdot \sigma \cdot S_{LFL} \cdot C_{L,max,L} \cdot \frac{m_{MTO}}{m_{ML}}$$

$$k_L = 0,107 \text{ kg/m}^3$$

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Preliminary Sizing – Take-Off



$$\frac{T_{TO}}{m_{TO} \cdot g} = \frac{k_{TO}}{\sigma \cdot C_{L,max,TO} \cdot S_{TOFL}} \frac{m_{TO}}{S_W} = a \cdot \frac{m_{TO}}{S_W}$$

$$a = \frac{k_{TO}}{\sigma \cdot C_{L,max,TO} \cdot S_{TOFL}}$$

$$k_{TO} = 2,34 \text{ m}^3/\text{kg}$$

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Preliminary Sizing – 2nd Segment

Start: retracted landing gear

End: altitude of 400 ft

Flaps: take-off configuration

**Req.: minimum climb gradient can be maintained
(with 1 inoperative engine)**

$$\frac{T_{TO}}{m_{MTO} \cdot g} = \frac{n_E}{n_E - 1} \left(\frac{1}{E} + \sin \gamma_{CLB} \right)$$

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Preliminary Sizing – Missed Approach

Abort landing → climb & turnaround

Flaps: landing configuration + extended landing gear

**Req.: minimum climb gradient can be maintained
(with 1 inoperative engine)**

$$\frac{T_{TO}}{m_{MTO} \cdot g} = \frac{n_E}{n_E - 1} \left(\frac{1}{E} + \sin \gamma_{MA} \right) \left(\frac{m_{ML}}{m_{MTO}} \right)$$

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Preliminary Sizing – Cruise

1. Thrust-to-weight ratio

Designed to reach destination (range)

Breguet range eq.:

$$R = \frac{V_{CR} \cdot E}{SFC} \cdot \ln \left(\frac{1}{1 - \frac{m_F}{m}} \right)$$

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Preliminary Sizing – Cruise

1. Thrust-to-weight ratio

→ Fly at minimum drag speed: V_{md} (E_{max})

→ Fly at max. range speed: V

$$\frac{T_{MTO}}{m_{MTO} \cdot g} = \frac{1}{\left(\frac{T_{CR}}{T_{TO}}\right) \cdot E}$$

$$\frac{T_{CR}}{T_{TO}} = (0,0013\mu - 0,0397) \frac{1}{km} \cdot h_{CR} - 0,0248\mu + 0,7125$$

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Preliminary Sizing – Cruise

2. Wing loading

Cruise: lift = weight

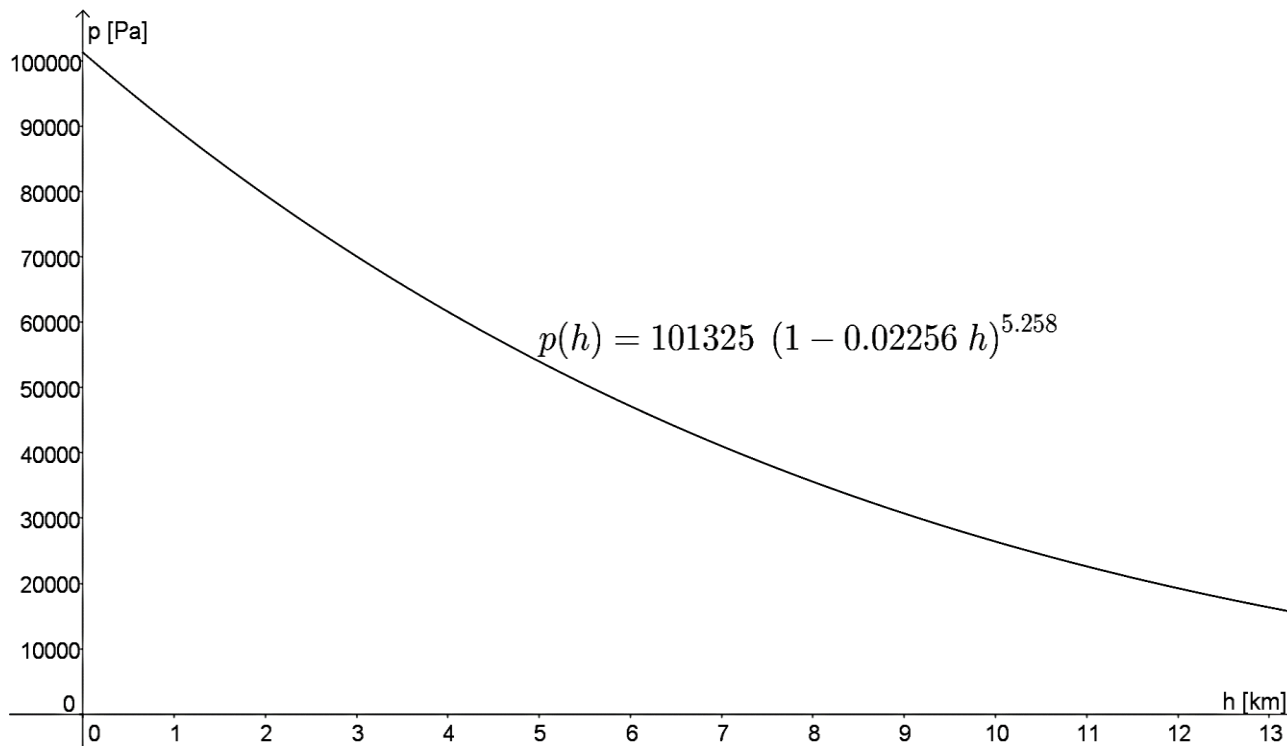
$$\frac{m_{MTO}}{S_W} = \frac{C_L \cdot M^2}{g} \cdot \frac{\gamma}{2} \cdot p(h)$$

$$\gamma = 1,4$$

Reverse Engineering of Passenger Jets – Classified Design Parameters

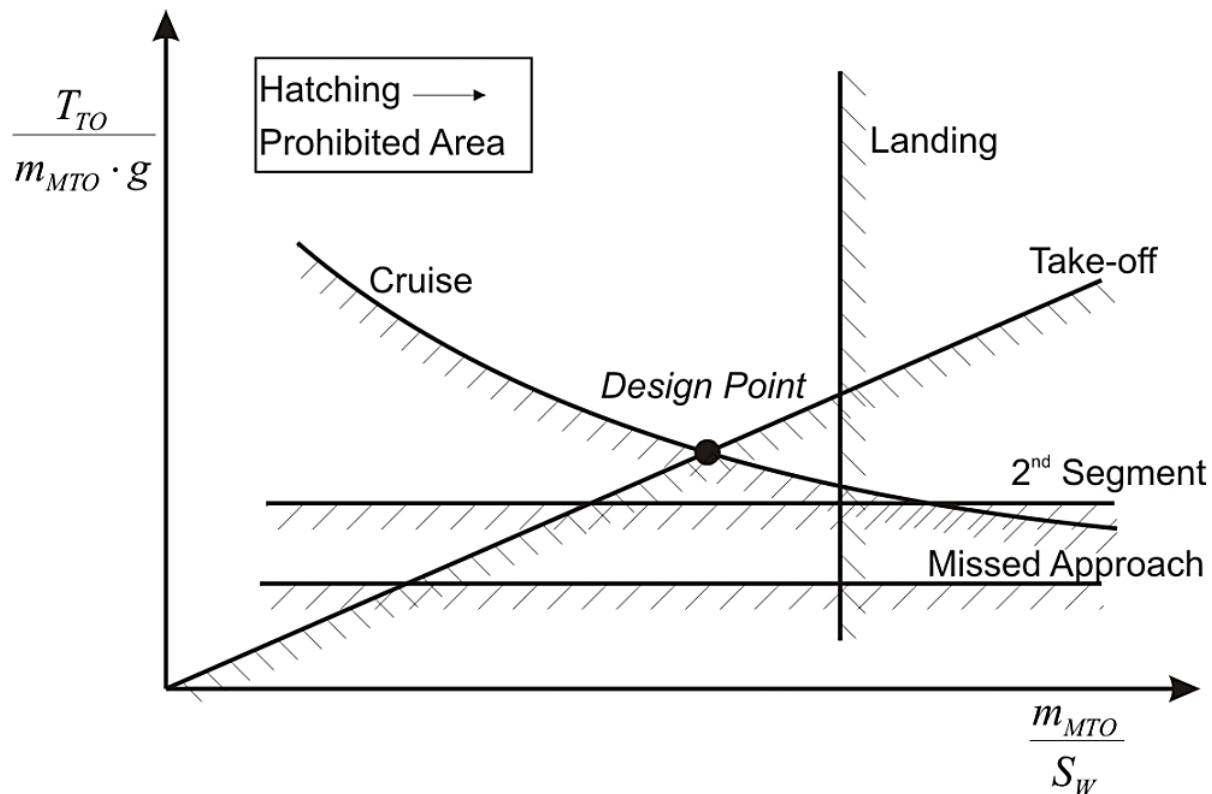
Preliminary Sizing – Cruise

2. Wing Loading



Reverse Engineering of Passenger Jets – Classified Design Parameters

Preliminary Sizing – Matching Chart



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

Def.: RE is a proces, used to understand the working of a product and to analyze its design

Provides documentation:

- **Specifications**
- **Mechanisms**
- **Materials**
- **Manufacturability**
- **Assembly details**

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Concept Reverse Engineering

RE is applied when technical data is:

- **Lost**
- **Not existing**
- **Property of another manufacturer**

Note: copyright!

Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

Black-box (hypothetical)



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

Black-box (hypothetical)



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

Black-box (hypothetical)



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

White-box



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

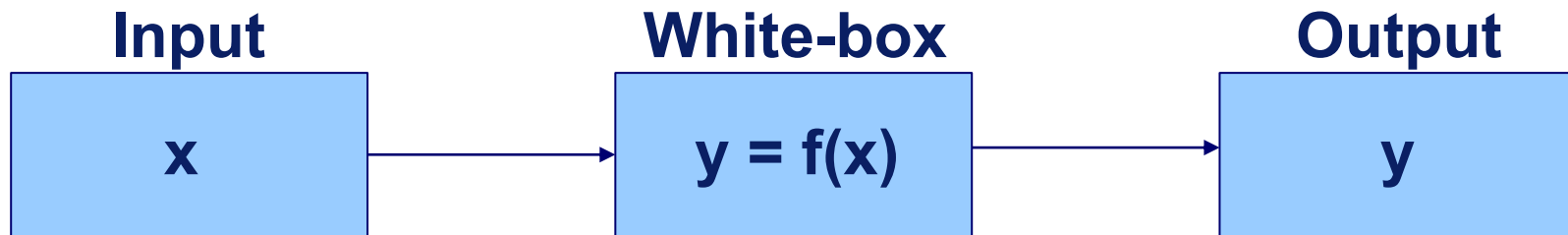
White-box



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

White-box



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

RE white-box



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

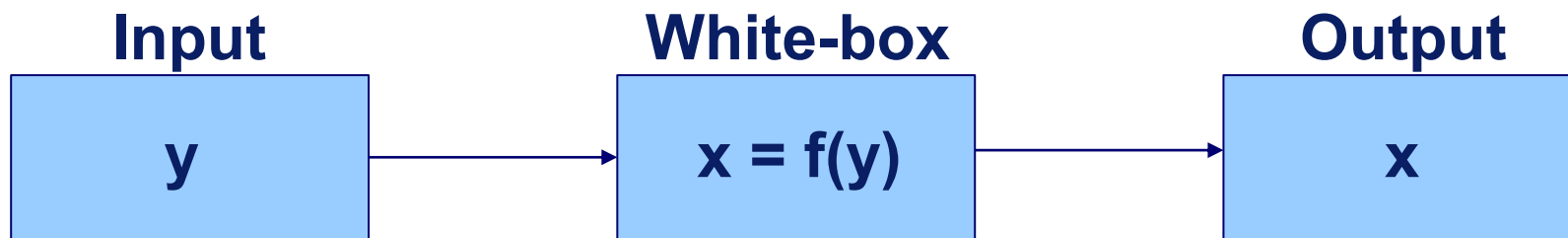
RE white-box



Reverse Engineering of Passenger Jets – Classified Design Parameters

Concept Reverse Engineering

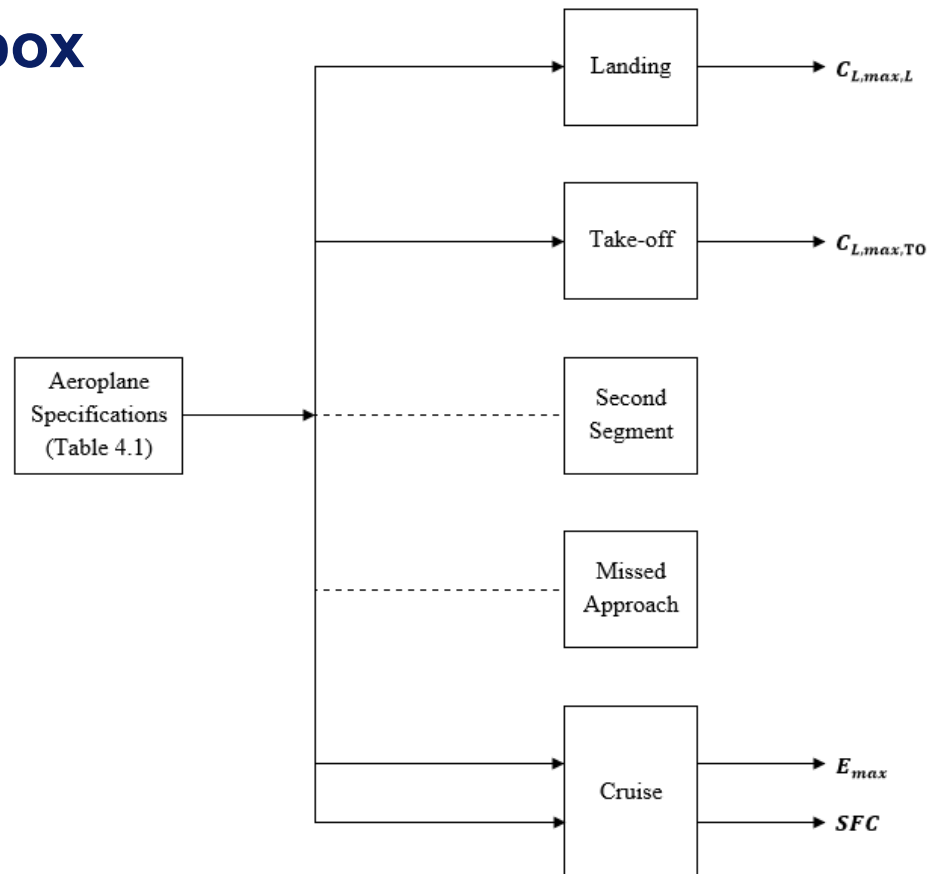
RE white-box



Reverse Engineering of Passenger Jets – Classified Design Parameters

Reverse Engineering of Preliminary Sizing

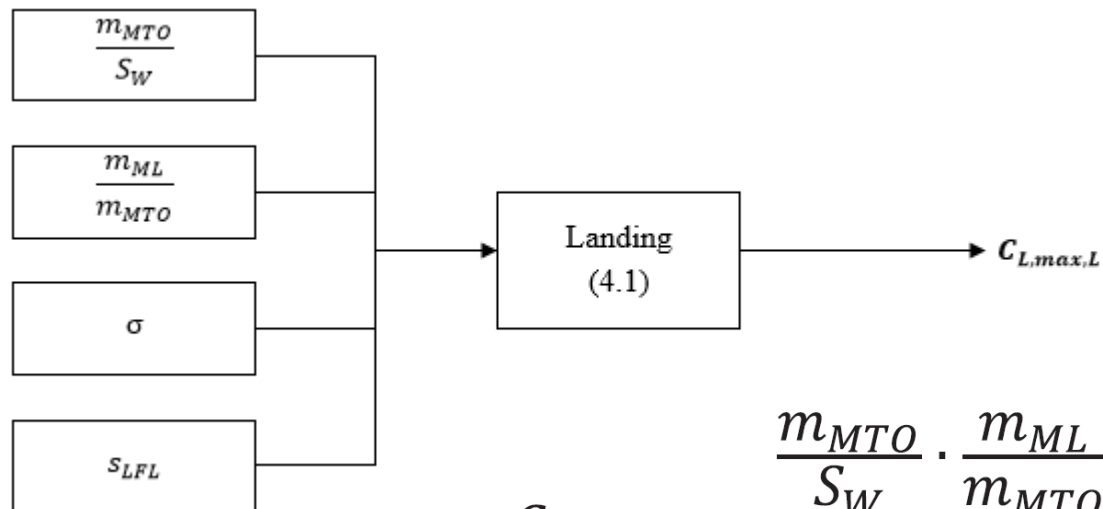
RE Black-box



Reverse Engineering of Passenger Jets – Classified Design Parameters

Reverse Engineering of Preliminary Sizing

RE white-box 1



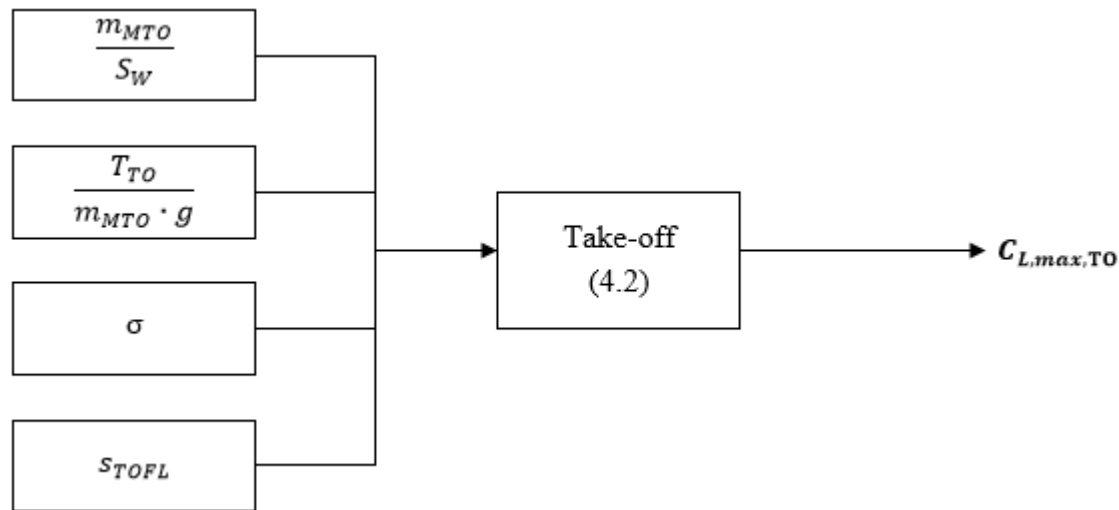
$$C_{L,max,L} = \frac{\frac{m_{MTO}}{S_W} \cdot \frac{m_{ML}}{m_{MTO}}}{k_L \cdot \sigma \cdot S_{LFL}}$$

$$k_L = 0,107 \text{ kg/m}^3$$

Reverse Engineering of Passenger Jets – Classified Design Parameters

Reverse Engineering of Preliminary Sizing

RE white-box 2

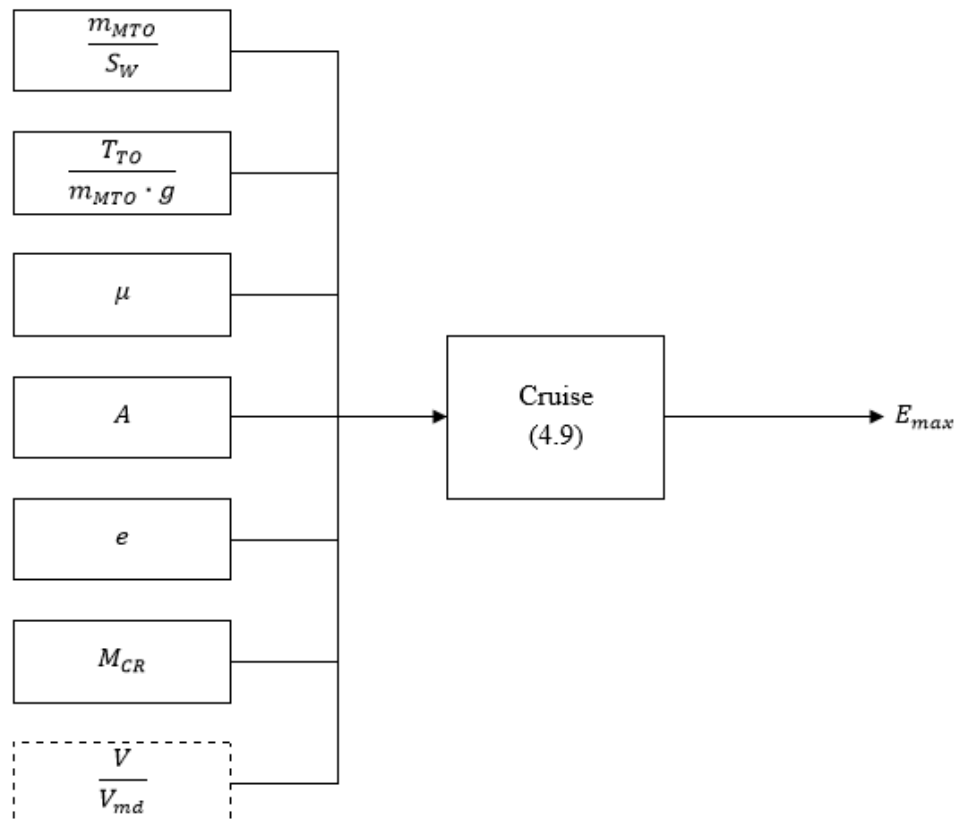


$$C_{L,max,TO} = \frac{k_{TO}}{\sigma \cdot S_{TOFL}} \cdot \frac{m_{MTO}/S_W}{T_{TO}/m_{TO} \cdot g}$$

Reverse Engineering of Passenger Jets – Classified Design Parameters

Reverse Engineering of Preliminary Sizing

RE white-box 3



Reverse Engineering of Passenger Jets – Classified Design Parameters

Reverse Engineering of Preliminary Sizing

RE white-box 3

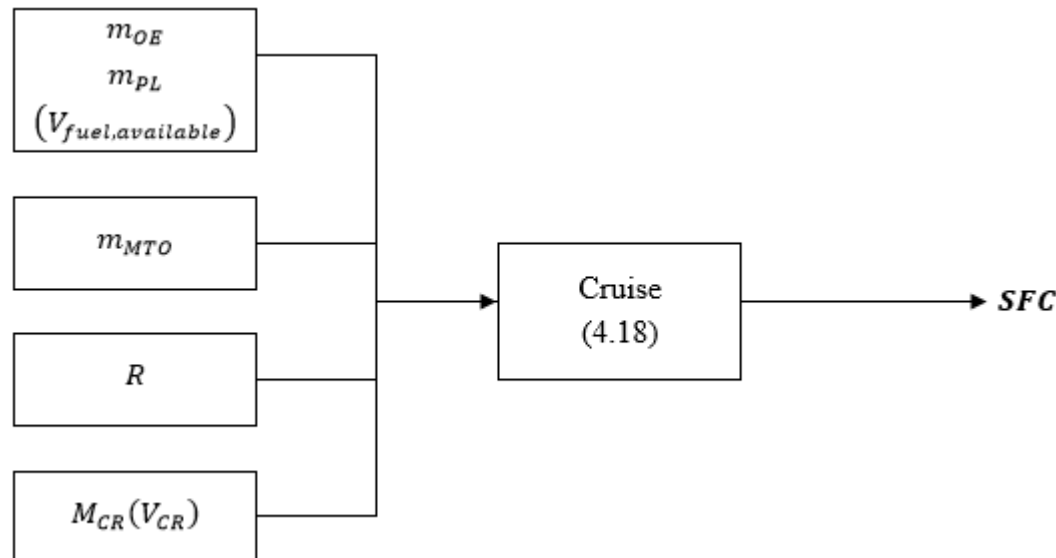
$$\frac{2 \cdot \frac{T_{TO}}{m_{MTO} \cdot g}}{\left(\frac{V}{V_{md}}\right)^2 + \left(\frac{V}{V_{md}}\right)^2} \left[E_{max}^{1,19} \cdot (0,0576\mu - 1,76) \cdot \left(\frac{4 \cdot g \cdot \frac{m_{MTO}}{S_W} \cdot \left(\frac{V}{V_{md}}\right)^2}{\pi \cdot A \cdot e \cdot M^2 \cdot \gamma \cdot p_0} \right)^{\frac{1}{5,258}} \right]$$

$$+ \frac{2 \cdot \frac{T_{TO}}{m_{MTO} \cdot g}}{\left(\frac{V}{V_{md}}\right)^2 + \left(\frac{V}{V_{md}}\right)^2} \cdot (-E_{max}) \cdot (0,0328\mu - 1,05) + 1 = 0$$

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Reverse Engineering of Preliminary Sizing

RE white-box 4



Reverse Engineering of Passenger Jets – Classified Design Parameters

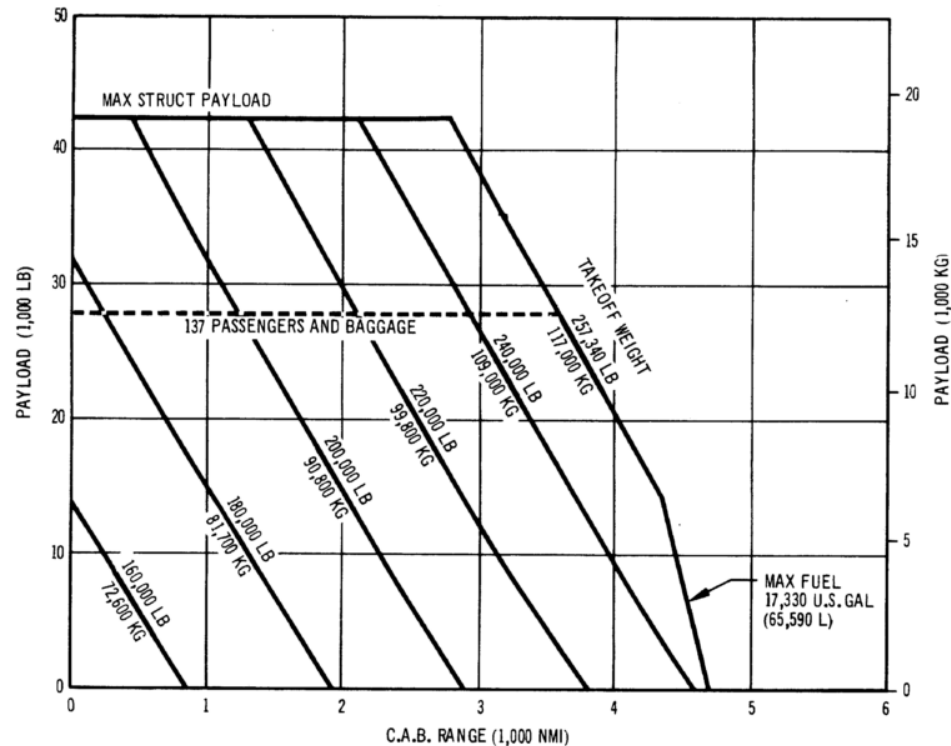
Reverse Engineering of Preliminary Sizing

RE white-box 4

$$SFC = \frac{E \cdot \ln \left(\frac{\frac{m_{PL}}{m_{MTO}} + \frac{m_{OE}}{m_{MTO}}}{M_{ff,TO} \cdot M_{ff,CLB}^2 \cdot M_{ff,DES}^2 \cdot M_{ff,L}} \right)}{g \cdot \left(\frac{R + S_{RES}}{V_{CR}} + t_{loiter} \right)}$$

Reverse Engineering of Preliminary Sizing

RE white-box 4



Reverse Engineering of Passenger Jets – Classified Design Parameters

Reverse Engineering of Preliminary Sizing

RE white-box 4

$$SFC = \frac{E \cdot \ln \left(\frac{1 - \frac{V_{fuel, capacity} \cdot \rho_{fuel}}{m_{MTO}}}{M_{ff, TO} \cdot M_{ff, CLB}^2 \cdot M_{ff, DES}^2 \cdot M_{ff, L} \cdot M_{ff, engine\ start} \cdot M_{ff, taxi}} \right)}{g \cdot \left(\frac{R + S_{RES}}{V_{CR}} + t_{loiter} \right)}$$

Reverse Engineering of Passenger Jets – Classified Design Parameters

The Tool

Necessity due to complexity:

- Amount of variables
- Mutual relations
- Numerical iteration
- Optimization solver

→ Tool: PJRE (Passenger Jet Reverse Engineering)





Reverse Engineering of Passenger Jets – Classified Design Parameters

The Tool

Requirements of PJRE

- **Accurate results**
- **Reliable results**
- **Quick**
- **User friendly**
- **Multifunctional**
- **Direct print-out**



Reverse Engineering of Passenger Jets – Classified Design Parameters

The Tool

Build-up

1. Specs + RE
2. C_{Lmax}
3. E_{max}
4. SFC
5. Matching Chart
6. Data
7. Verification

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The Tool

Demonstration A320-200 (Airbus)



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Example BAe 146-200 (British Aerospace)



Reverse Engineering of Passenger Jets – Classified Design Parameters

Example BAe 146-200 (British Aerospace)

Google: 'Airport planning' + aircraft manufacturer

<https://www.skybrary.aero/index.php/Category:Aircraft>

<https://booksite.elsevier.com/9780340741528/appendices/data-a/default.htm>

<https://booksite.elsevier.com/9780340741528/appendices/data-b/default.htm>

<http://www.jet-engine.net/>

Note: mission fuel fraction for climb = 0,998!

Reverse Engineering of Passenger Jets – Classified Design Parameters

Example BAe 146-200 (British Aerospace)

- $C_{L,max,L} = 3,62$
- $C_{L,max,TO} = 2,63$
- $E_{max} = 14,5$
- $SFC = 19,5 \text{ mg/N/s}$



Reverse Engineering of Passenger Jets – Classified Design Parameters

Example BAe 146-200 (British Aerospace)



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Reverse Engineering of Passenger Jets – Classified Design Parameters

PJRE

Positive

- Quick
- Reliable
- Accurate
- Multifunctional
- Reduces complexity
- User friendly

Negative

- Only (large) passenger jets
- Sensitive to human error
- Critical view